

# **TrueStructures**<sup>™</sup>

### Strain Analysis System

## Operator's Manual and Sample Lab Procedure



TrueStructures<sup>TM</sup> Strain Analysis System shown with I-Beam, Torsion Tube and Airfoil-Shaped Test Structures, Virtual Instrument Panel Displays

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TrueStructures<sup>™</sup> Strain Analysis System shown with all test structures

#### Introduction to Strain Data Acquisition and Analysis

In this lesson (which will include Lesson #1: Introductory Measurement Exercise on Page 17), we will familiarize ourselves with the TrueStructures<sup>™</sup> System. The knowledge gained will be the basis for all future analysis opportunities.

#### System Components

#### Rigid Frame

The system frame is a very rigid steel structure which will provide the proper strength to support the experimentation without deflection. It is designed to accommodate a number of primary structural members for analysis. NOTE: See page 18 for caster adjustment photo if unit is on uneven floor.

#### Test Structures

The TrueStructures<sup>™</sup> System includes the following structures for analysis:

- I-Beam: A very capable basic load supporting structure.
- Tube: A very important configuration for structures and drive shafts.
- Aircraft Airfoil: An advanced structure building on the basic I-Beam and Tube analysis.



I-Beam Test Structure

Torsion-Tube Test Structure



Note: The aircraft airfoil used in this lab is actually half of a horizontal stabilizer from a production aircraft. While the structure is essentially the same as an aircraft wing, the size allows the system to comfortably fit in the test frame and makes it more affordable.

Airfoil Test Structure

#### Applying Load to Test Structure

Utilizing a crank mechanism and adjustable position load cell, a force or load can be applied to the structure specimen.

- In regards to the wing structure, the force can be applied anywhere along the end of the wing from the front spar to behind the trailing edge of the wing. This force causes the normally cantilevered position of the wing at rest to take on bending or combination bending and torsional loads that might be encountered in flight, or upon landing.
- In regards to I-Beam and Tube test structures, the point load can be positioned at the centerline of each specimen.



Load Cell under Torque Arm

#### Load Cell

Applies and measures force applied to test specimen. Signal sent to on-board National Instruments Data Acquisition System and LabView<sup>TM</sup> generated virtual instrument panel (VI).

#### **Position Scales**

Graduated scales applied to the frame. Indicates position of Load Cell Point Load Applicator along x-axis and deflection of test specimen due to loading along y-axis.

Adjustable Point Load Position Table Enables load cell to be positioned at an infinite number of positions for variable loading scenarios. Utilizes friction clamp to lock table into desired position.

#### Angle Drive Crank Mechanism

Raises and lowers load cell platform for load application. Includes preset maximum load clutch to prevent system overload.





#### **Strain Gages**

Strategically-placed measurement devices used to provide strain data.



Uni-Axial Strain Gage



Strain gages are essentially grid shaped metallic wire, foil, or semiconductor materials that are bonded to the surface they are measuring by a carrier matrix and a thin insulating layer of adhesive. When the carrier matrix is strained, the strain is transmitted to the metallic grid through the adhesive, essentially deforming the grid and changing its electrical resistance. Variations in the electrical resistance of the grid are measured as an indication of strain. Each structural element contains two different types of strain gages: uni-axial and tri-axial rosette style (as pictured above). Each lesson will illustrate the structure being tested along with the location, type and identification letter of each individual strain gage.



Strain Gage placement on I-Beam Test Section

Each strain gage on each test section is connected electrically to a National Instruments Data Acquisition System.



Torsion Tube Strain Gage Layout with Multi-Pin Connection Box

The gage arrays are terminated on a quick disconnect multi-pin connector box.



Multi-Pin Connection Box and Cord

When the multi-pin connector is connected...



Twist-On/Twist-Off Multi-Pin Connection

the strain gages are now electrically connected to a National Instruments<sup>™</sup> Compact Data Acquisition System.



Connections into Data Acquisition Box

#### **Data Acquisition**

The data acquisition system accommodates the twelve system strain gage inputs on modules 1 & 2, with a load cell input (applied load measurement) on module 3. Slot 4 is open and available for expansion.



Data Acquisition Enclosure with DAQ Module Configuration

#### Virtual Instrument Panel

The Data Acquisition System then sends output to a LabView<sup>™</sup> Generated Virtual Instrument Panel hosted on a system laptop computer.



Data Acquisition System Connected to Lap-Top Computer

Each test structure has its own Virtual Instrument display. Here is a front display showing the I-Beam test structure and its loading criteria; cantilever pure bending.



I-Beam Loading Screen

Tabs along the top of the screen allow the operator to choose which structure they have loaded in the test fixture, plot data and calibrate each strain gage channel. This particular screen is the I-Beam in bending (the I-Beam Tab is on). Notice there are tabs for:

- Airfoil
- Tube-Bending
- Tube-Torsion
- Tube-Combination
- Plot Data
- Calibration.

Each strain gage mounted to that particular test structure is displayed along with its strain value as the specimen is loaded. In this case, there are 7 strain gages, labeled A through G, displayed.

Structure loading is indicated by a sliding "Load" graphic right below the structure graphic.

Tabs along the bottom allow you to:

- Stop/Start Program
- Pause Program
- Log Data to a File
- Export a Screenshot

• Change Data Sample Rate

When you press the Plot Data Tab, the data plot screen is displayed;

Turbine Techno	logies, Ltd.		11:24:54 AM 11/16/2015	8	True	Structures™
Airfoil	I - Beam	Tube - Bending	Tube - Torsion Tu	ibe - Combination	Plot Data	Calibration
Strain Guage A Strain Guage B Strain Guage C Strain Guage C Strain Guage C Strain Guage C Strain Guage F Strain Guage F Strain Guage H Strain Guage I Strain Guage J Strain Guage K Strain Guage L Strain Guage L	7.00E+1- 6.00E+1- 5.00E+1- 3.00E+1- 2.00E+1- 1.00E+1- 0.00E+0- -1.00E+1- -2.00E+1- -3.00E+1- -3.00E+1- -5.00E+1- -7.00E+1- -7.00E+1-					
Strain & 11	0 2	4 6 8 10	12 14 16 18 20 22 24 Dat	26 28 30 32 ta Point	34 36 38 40 42	44 46 48 50 51
Strain Gage A -62.64 JL Strain Gage G -14.38 JL	Strain Gage B 61.95 JL Strain Gage H 0.00 JL	Strain Gage C 28.02 JL Strain Gage I 0100 IL	Load o 5 10 15 20 25 30 35 40 45 50 tbs 40.6 lbs	Strain Gage D -33.38 JL Strain Gage J 0.00 JL	Strain Gage E 12.87 µ Strain Gage K 0.00 µ	Strain Gage F -1.83 JL Strain Gage L 0.00 JL
X Stop Progra	am	Pause	Log Data to File	Export Sc	reenshot	1 Sample/sec

I-Beam Strain Plot Data Screen

Each active strain channel on the left-hand column is checked and displays the color-coded line used in the live strain graph.

The graph itself plots the strain reaction to the applied load. Over a period of time listed as data points.

The loading graphic from the front screen resides in the section right below the graph. Individual strain values for each strain gage channel are also displayed. Along the bottom, you still have the tabs indicating;

- Stop/Start Program
- Pause Program
- Log Data to a File
- Export a Screenshot
- Change Data Sample Rate



If you click on the Calibration tab along the top of the screen, you get the following;

**Step 1:** Press **Tare** button. This zero's out any values in the strain gages that have no load on them. Those that are loaded in the current test specimen at rest will show the value of that loading at rest.

Step 2: The Load Offset window may show a load. Use arrows to zero that load.

#### Step 3: Click Save Sensor Calibration

The next test structure screens cover the Torsion Tube. There are three front screens for the Torsion Tube as there are three separate configurations for this structure.

The first configuration is Pure Bending. The Tube is mounted in a cantilever position and a load is applied in a pure bending mode.



Torsion Tube Pure Bending Loading Screen



Torsion Tube Pure Bending Strain Plot Data Screen

The second configuration for the torsion tube is pure torsion. A rotational yoke (red "A-frame" device in screen shot) is applied to the end of the tube to restrict its motion to pure torsion when a torsional load is applied.



Torsion Tube Pure Torsion Loading Screen



Torsion Tube Pure Torsion Strain Plot Data

The third configuration for the torsion tube is combination loading. This is accomplished by removing the rotational yoke and applying a torsional load. This creates combination bending and torsional forces on the structure.



Torsion Tube Combination Loading Screen



Torsion Tube Combination Loading Strain Plot Data Screen

The next test specimen screens cover the airfoil. The airfoil is a more sophisticated progression of the combination of the I-Beam and Tube. Essentially the two internal spars are analogous to I-Beams, while the outer skin can be likened to an airfoil-shaped tube. The load cell used to apply loads on the structure can be positioned anywhere along the chord of the airfoil (profile view), allowing pure bending and various combination bending scenarios.



Airfoil Loading Screen



Airfoil Strain Plot Data Screen

#### LAB LESSON #1: Introductory Measurement Exercise

For this exercise, we will use the TrueStructures<sup>™</sup> Airfoil (Wing) Structure. If the wing is not installed, please install it as shown.



Position wing to align spar ends with fixture tangs.



Finger-tighten knobs. Lift up on cantilever end of wing to remove any sag in system. Tighten knobs firmly while continuing to lift end of wing.



on Data Acquisition Box.

**Step 1.** Turn on the Data Acquisition Box. If you wheeled the unit in from a colder place, let the unit acclimate to room temperature first as strain gages are sensitive to temperature changes and can produce inconsistent readings.

Step 2. Bring up the Load Screen Virtual Instrument Panel on your computer.

NOTE: Because of the weight of the wing test section, there is play in the end of the wing after it is secured on the capture end. Before you start the test, lift up on the free end of the wing to remove any remaining "sag" and then crank up the load cell to the point of application so that it just touches the wing bottom. This will give you a more accurate starting point and deflection amount. Adjust system casters, as shown below, if floor surface is uneven.



Lift to remove any sag.



Caster Adjustment.

**Step 3.** Now, add a load to the system. This is accomplished by loosening the friction lock and sliding the Load Cell Point Load Applicator until it is positioned directly under the point of interest. In this exercise, position it in the middle of the front spar of the wing (see below).



Loosen friction lock to position load cell.



Position Load Cell at Wing Main Spar Position

#### **Step 5.** Tighten the friction lock.



Friction Lock



Load Wheel

**Step 6.** Using crank handle, start cranking clockwise to add a load to the wing endplate structure. For this exercise, add a net 50 pounds (compensating for any initial value on the display). Follow the load application display on the Virtual Instrument Panel. Allow readings to settle for 10-15 seconds. Then hit "Log Data to File" button on the lower part of the screen, save it and then try reducing loads incrementally and recording the information for a strain progression data set.



Airfoil Loading Screen



Airfoil Plot Data Screen

**<u>Step 7</u>**: As you go through the loading steps, hit the Plot Data Tab to view the strain values of each strain gage as loading is changed. When you desire to apply more load, jump back to the Airfoil tab and watch the Load values being applied.

### How Strain Is Calculated

Where did these numbers come from?

Let's start with the basics. Strain is measured using a **Wheatstone Bridge Circuit** in the Data Acquisition System. Each strain gage on the test specimens are one of four resistors that make up the Wheatstone Bridge Circuit.



Wheatstone Bridge Circuit

A known input voltage feeds all four resistors in the system: If all four resistors have the same resistance, the output voltage (Vout) will match the input voltage (Vin) in a balanced circuit.

In our situation, 3 known resistors of 350 Ohms are fixed in the Data Acquisition Box while the fourth resistor to round out the bridge circuit is the particular strain gage of interest. The shape of the strain gage (whether at rest or in a compressive or tensile loading condition) causes a certain resistance value, which changes the voltage output of the bridge circuit. As the gage is strained, its resistance changes, changing the output voltage of the circuit.

The change in resistance of the strain gage and resultant unbalanced voltage output of the bridge circuit is the basis for strain measurement data.

#### Vout = Vin [ R3/(R3 + Rg) - R2/(R1+R2)]

Manufacturers of strain gages build in certain characteristics which allow steady, reliable readings from their strain gages. Gage Factor is one of those items. Essentially, the Gage Factor relates the ratio of the change in resistance with respect to initial resistance directly to the Strain Value. This is also known as strain sensitivity.



Where  $\bigwedge Rg$  = strained value of gage resistance

Rg = unstrained value of gage resistance

 $\boldsymbol{\mathcal{E}}$  = Resulting Strain

The Gage Factor for your systems strain gages is shown on your Strain Calculator.

Now you have a feel for how to gather strain data and where the numbers come from. However, jumping into an analysis of an aircraft wing is sort of like jumping right into your PhD in engineering right out of high school. In the next couple of lab sessions, we'll analyze some basic structures to gain a fundamental understanding of the primary elements of strain on a structure. This will allow you to better understand the analysis of an aircraft wing.

LAB SESSION #2: The I-Beam in Bending In this session, we will analyze a standard 6061-T6 Aluminum I-Beam using the TrueStructures<sup>TM</sup> System to place a pure bending load on it.



Loading and Strain Gage Placement/Identification

Setup Note: I-Beam should be mounted in the frame and strain gages electrically connected to the Data Box as shown below. If another element such as the Wing or Hollow Circular Shaft is currently in the frame, it should be carefully removed and stored.



Position I-Beam Assembly onto Frame



Apply and finger-tighten connection knobs. Pull up on cantilever end of beam to remove any sag and tighten knobs while pulling up on beam.



Tighten end bolts for sag-free connection.

**Step 1.** Position the load cell directly under the central vertical axis of the I-beam. Tighten friction clamp.

**Step 2.** Open up the Virtual Instrument program on the laptop computer. Go to Calibration Screen and hit Tare Button to zero out readings.

**Step 3**. Crank load cell up until it touches the bottom of the beam; note vertical position on deflection scale. Load reading display should read zero. Now, crank in 50 lbs of load. Note new vertical position on scale (this is your tip deflection).



Plug in Data Box Multi-Pin Connector.



Position load cell under center of I-Beam



I-Beam Loading Screen

**Step 4**. Go to the Plot Data Screen to see the strain value plots based on the actual loading.

**Step 5.** Measure the beam cross section and determine its Area Moment of Inertia. Why do we need to know this?

**Step 6.** Calculate the Section Modulus for the I-Beam (provide just a neutral axis calculation for this step to show your methodology). Why is this important?

Step 7. Determine the Modulus of Elasticity? Why is this important?

Step 8. Draw the Load, Shear and Bending Diagrams for this scenario.

**Step 9.** Calculate the theoretical normal stresses due to bending at each mid-span uniaxial strain gage location. Where do the highest normal stresses occur: web or flanges?

**Step 10.** Now, use your answers from Step 9 to calculate the theoretical normal strains at each uniaxial train gage location.

**Step 11.** Compare actual strain readings to theoretical calculations by plotting those values against the corresponding uni-axial strain gage positions on the I-Beam.

**Step 12.** Let's now consider our shear stresses due to bending. Calculate the theoretical shear stresses at each mid span uni-axial strain gage location and at the neutral axis of the beam (where is neutral axis and how is it determined?).

**Step 13.** Plot these values to show a shear distribution on the I-Beam. Where does a majority of the shear stress occur; web or flanges?

#### Advanced Analysis

**Step 14**. Using the readings from the rosette strain gages, determine the shear strain at the neutral axis. You will want to use the rosette equations developed for your particular rosette strain gage configuration (rectangular) and then utilize Mohr's Circe to plot the principle strains. How do your measured shear strains compare with the results of the theoretically calculated shear strains?

#### **Extra Analysis**

**Step 15**. Based on the loading, what is the shear flow of this beam cross-section? What is the consequence of shear flow in this particular application?

#### Lab Session #3 Hollow Shaft (Tube) Analysis

In this session, we will analyze a standard 6061-TL Aluminum tube using the TrueStructures<sup>TM</sup> System to place it in:

- pure bending
- pure torsion
- combination bending and torsion.

Hollow circular shafts (tubes) are used in static, rigid structures such as tubular bicycle frames and in dynamic, power transfer structures such as drive shafts. A good basic understanding of the load carrying capabilities of a tube will provide insight into more complicated structures such as an aircraft wing.

#### **Exercise A: Pure Bending Analysis**

Place the hollow shaft in pure bending.



Loading and Strain Gage Placement/Identification

<u>Setup Note</u>: Hollow Shaft should be mounted in the frame and strain gages electrically connected to the Data Acquisition box through the Multi-Pin Connector. If another element such as the Wing or I-Beam is currently mounted in the frame, it should be carefully removed and stored. Please see the appropriate section of this manual for installation and removal instructions of any particular test section.



Position tube on frame as shown.



Secure block end with capture knobs while pulling up on cantilever end to remove sag.



Insert Cantilever Load Block on red end.



Tighten Load Block with Allen Wrench.

**Step 1.** Measure the hollow shaft cross section and determine its Area Moment of Inertia. Why do we need to know this?

Step 2. Determine the Modulus of Elasticity? Why is this important?

Step 3. Calculate the Section Modulus for the Hollow Shaft. Why is this important?

**Step 4.** Position the load cell directly under the central vertical axis of the Hollow Shaft.

**Step 5.** Open up Virtual Instrument program on your computer to Tube Bending Tab. Go to Calibration Screen and hit Tare Button to zero out readings.

**Step 6**. Crank load cell up until it touches bottom of the tube. Note vertical position on scale. Load reading display should read zero. Crank in 50 lbs of load. Note new vertical position on scale (this is tip deflection).

**Step 7**. Click on Plot Data tab to see strain Data plots. Save your data.



Position load cell at tube centerline.



Tube Pure Bending Load Screen

Turbine Techno	logies, Ltd.	11	I:16:32 AM 11/16/201	5	True	Structures™
Airfoil	I - Beam	Tube - Bending	Tube - Torsion	Tube - Combination	Plot Data	Calibration
Strain Guage A Strain Guage B Strain Guage C Strain Guage C Strain Guage C Strain Guage F Strain Guage F Strain Guage F Strain Guage I Strain Guage I Strain Guage L Strain Guage L Data Point	1.75E+2- 1.50E+2- 1.25E+2- 1.00E+2- 7.50E+1- 5.00E+1- 2.50E+1- 2.50E+1- -5.00E+1- -5.00E+1- -7.50E+1- -1.00E+2- -1.25E+2- -1.75E+2- -1.75E+2- 0 1	2 3 4 5 6 7 8	9 10 11 12 13 14 15 1		24 25 26 27 28 29 3	30 31 32 33 34 35
Strain Gage A	Strain Gage B	Strain Gage C	Load	Strain Gage D	Strain Gage F	Strain Gage F
-145.73 µ Strain Gage G 14.86 µ	145.21 μ Strain Gage H 11.98 μ	Strain Gage I	ο΄ ἐ τὸ τἱς ἐὸ ἐἐς ἐἰς ἀ ψ Ibs 40.8 Ibs	so Strain Gage J 0.00 μ	-14.54 μ Strain Gage K 0.00 μ	-2.09 JL Strain Gage L 0.00 JL
X Stop Progra	ım	Pause	Log Data to File	e Export Scre	eenshot	I Sample/sec

Torsion Tube Pure Bending Strain Plot Data

Step 8. Draw the Load, Shear and Bending Diagrams for this scenario.

**Step 9.** Calculate the theoretical normal and shear stresses due to bending at each midspan strain gage location.

**Step 10.** Now, use your answers from Step 9 to calculate the theoretical normal and shear strains at each strain gage location.

**Step 11.** Compare actual strain readings to theoretical calculations by plotting those values against the corresponding strain gage positions on the tube.

#### Advanced Analysis

**Step 12**. Use Mohr's Circle Analysis to verify the above calculations and to plot the resulting bending and shear strains at each strain gage rosette mounted on the neutral axis of the tube. Verify the corresponding bending and shear stresses from this analysis and compare with the theoretical values calculated. These results will be important as comparison values for future loading of the tube in pure torsion and finally compound bending and torsion of the tube.

**Step 13**. Compare the resulting loading, stress, strain of the tube with that of the I-Beam for the applied load. What conclusions can be drawn from the analysis regarding suitability of a Tube verses I-Beam for a cantilever bending situation?

**Step 14**. Based on the loading, what is the shear flow of this tube cross-section? What is the consequence of shear flow in this particular application?

#### **Exercise B: Pure Torsional Analysis**

This exercise will apply pure torsional loading to a typical circular drive shaft which is restrained from bending on both ends. We are concerned with Shear Stress and Shear Strain in torsion with this type of shaft configuration.



Loading and Strain Gage Placement/Identification

**Setup Note**: Hollow Shaft with Torsion Yoke End will be mounted in the frame and strain gages electrically connected to the Data Acquisition Box with Multi-Pin connector. If the Wing or I-Beam is currently mounted in the frame, it should be carefully removed and stored. If you still have the tube mounted in the structure in the cantilever position with the load block on the end from the previous exercise, remove the load block, then remove the tube from the frame, reversing the process shown in the previous exercise (Exercise A). Then follow the new instructions below:



Position Yoke on Crank End (note correct face out as marked)



Align with frame holes and loosely secure with capture knobs (do not tighten yet).



Slide red end of tube into yoke. Push in fully.



Tighten block end knobs fully. Then tighten red yoke knobs securely.



Position guide pins and slide on Torque Arm



*Tighten Torque Arm Bolt securely with Allen Wrench.* 



Position Load Cell to desired moment arm dimension from tube centerline (Step 2).



Crank in load and take readings on each channel (Steps 3, 4).

**Step 1.** Measure the hollow shaft cross section and determine its Polar Moment of Inertia. What is Polar Moment of Inertia and why do we need to know this?

**Step 2.** Position load cell directly under the torsional loading arm axis of the Hollow Shaft as shown. Measure and record the moment arm from center of Hollow Shaft to load cell application point.

**Step 3.** Open up Virtual Instrument Panel on your computer, click on Tube-Torsion Tab. Go to Calibration Screen and hit TARE to zero-out strain gages. Click on Tube-Torsion Tab again.

**Step 4**. Crank load cell up until it touches the bottom of the torsional loading arm; note vertical position on scale. Load reading display on should read zero. Now crank in 50 lbs of load.



**Step 5**. Click on Data Plot tab to observe the strain loading plots.

Torsion Tube Pure Torsion Load Screen

Turbine Techno	logies, Ltd.		9:19:15 AM 11/17/2015		Trues	Structures™
Airfoil	I - Beam	Tube - Bending	Tube - Torsion Tu	ibe - Combination	Plot Data	Calibration
Strain Guage A	3.50E+1-					
Strain Guage B	3.00E+1-					
Strain Guage C	2.50E+1-					
Strain Guage D	2.00E+1-					
Strain Guage E	1.50E+1-					
Strain Guage E	1.00E+1-					100 C
Strain Guage G	0.00E+0-					
Strain Guage H	5.00E+0-					
Strain Guage I	-1.00E+1-					
Strain Guage I	-1.50E+1-					
Strain Guage K	-2.00E+1-					
Strain Guage K	-2.50E+1-					
Strain Guage L	-3.00E+1-					
Data Point 💩 🕮 🚛	-3.50E+1-	4 6 8 10 12 14	16 18 20 22 24 26 28 30 32	34 36 38 40 42 44	46 48 50 52 54 56	58 60 62 64 67
Strain & II	0 2	4 0 0 10 12 14	Dat	ta Point	40 40 50 52 54 50	>0 00 02 04 07
Strain Gage A	Strain Gage B	Strain Gage C	Load	Strain Gage D	Strain Gage E	Strain Gage F
-2.75 JL	6.65 JL	27.36 JL		-3.26 μ	-30.44 μ	31.57 JL
Strain Gage G	Strain Gage H	Strain Gage I	0 5 10 15 20 25 30 35 40 45 50	Strain Gage J	Strain Gage K	Strain Gage L
5.88 JL	-25.65 µ	0.00 [1]	५ lbs 39.8 lbs	0.00 µ	0.00 JL	0.00 JL
Stop Progra	am III	Pause	Log Data to File	Export Scr	enshot	Sample/sec
- Stop Progra		Tause		Export Sert		Jumpioraec

Torsion Tube Pure Torsion Data Plot Screen

#### Further Analysis

Step 6. Sketch the loading diagrams for this scenario.

Step 7. Determine the Shear Modulus of Elasticity? Why is this important?

**Step 8.** Calculate the Maximum Torsional Shear Stress experienced by the shaft under this loading Why is this important?

**Step 9:** Let's analyze the shear strain of our hollow shaft using Mohr's Circle as it applies to our rosette strain gage. The analysis is based on the clock-wise orientation of the rosette as positioned along the straight outer skin line. We use a rosette to compute the state of strain at that particular point. The resulting Mohr's Circle plot gives the value and orientation of the principle strains. The uni-axial strain gages react only to the shear stress in this configuration (as there is no bending). It will be important to compare the differences in the uni-axial strain gage readings with our next configuration (combination loading).

#### Additional Analysis

**Step 10**. Let's calculate the torsional deflection (twist) of the shaft between the strain gage location and applied torque position for the loading shown.

**Step 11**. Shear Stresses due to torsion on a closed element such as a hollow shaft or tube act around its cross-sectional perimeter. This is known as the Shear Flow for this configuration. Calculate the Shear Flow for the tube with current loading.

#### Exercise C: Combination Loading: Bending and Torsion

For this exercise, we will remove the torsional end Yoke from the pure torsion configuration to return the hollow circular shaft (tube) to a cantilever configuration. We will load the tube in torsion, as in Lesson B. However, as you will see, the tube will now absorb combination bending and torsion, a more demanding load configuration. This cantilever configuration will be compared with the previously restrained configuration to show the differences in these two scenarios.



Loading and Strain Gage Placement/Identification

<u>Setup Note</u>: Tube should be mounted in the frame and strain gages electrically connected to the Data Acquisition Box through the Multi-Pin Connection. If another element such as the Wing or I-Beam is currently mounted in the frame, it should be carefully removed and stored.

**Important:** Please be sure torsional end Yoke is removed from load end of tube before starting this analysis. Please follow the removal instructions on the next page.



Loosen Torque Arm with Allen Wrench and remove.



Loosen capture knobs, remove yoke.



Insert Torque Arm into Tube End.



Loosen capture knobs on capture block end and slide tube out of yoke.

![](_page_36_Picture_10.jpeg)

Position tube in cantilever position, tighten hand knobs while pulling up on tube end..

![](_page_36_Picture_12.jpeg)

Tighten Arm with Socket Wrench, then position Load Cell.

#### Note: Turn the system on to allow acclimation if it has been off.

**Step 1.** Record the Polar and Area Moments of Inertia for the tube cross-section. Why do we need both of these?

**Step 2.** Position the load cell directly under the torsional loading arm axis of the Tube as shown. Measure the moment arm from center of Tube to load cell application point (use the same value as the previous exercise).

Step 3. Open up Virtual Instrument Panel on your computer. Click on Tube-Combo Tab

**Step 4**. Crank load cell up until it touches the bottom of the torsional loading arm. Go to Calibration Screen and hit TARE to zero out all strain readings. Return to Tube-Combo screen. Note vertical scale position on frame. Load reading display should read zero. Now crank in 50 lbs of load.

#### Note: If there is some sag in the test section, pull up on red end of tube to remove the sag. While holding the tube in this spot, position the load cell so it just touches the bottom of the torque arm. Start your test from this position.

**Step 5**. Go back Data Plot Screen and observe strain value plots. Unlike pure torsion, where our main focus was the strain gage rosettes, we will be very interested in all gages because of the added bending due to cantilever state of the hollow shaft.

![](_page_37_Figure_9.jpeg)

Torsion Tube Combination Loading Screen

Turbine Techno	logies, Ltd.	11	:13:23 AM 11/16/20	15	True	Structures
Airfoil	I - Beam	Tube - Bending	Tube - Torsion	Tube - Combination	Plot Data	Calibration
🗹 Strain Guage A	1.50E+2-					
🗹 Strain Guage B 📉	1.25E+2-					
🗹 Strain Guage C 🔼	1.00E+2-					
🗹 Strain Guage D 🌇	7.50E+1-					
🗹 Strain Guage E  📉	5.00E+1-					
🗹 Strain Guage F	2.50E+1-					
🗹 Strain Guage G 🛛 🥂	0.00E+0-					
Strain Guage H	5 00E+1-					
Strain Guage I	-7.50E+1-					
Strain Guage J	-1.00E+2-					
🗆 Strain Guage K	-1.25E+2-					
🗆 Strain Guage L 🛛 🔨 🗸	-1.50E+2-					
Data Point & 12 *.**	-1.75E+2-					
Causia 0 11 1.17	0 1	2 3 4 5 6 7 8	9 10 11 12 13 14 15 16	17 18 19 20 21 22 23 24 2	25 26 27 28 29 30 31 3	32 33 34 35 36 3
Strain Gage A	Strain Gage B	Strain Gage C	Load	Strain Gage D	Strain Gage E	Strain Gage F
-146.85	145.09 JL	34.43 LL		-17.84 [1	-46.38 LL	28.83
	Strain Gage H	Strain Gage I	0 5 10 15 20 25 30 35 40 4	5 50 Strain Gage J	Strain Gage K	Strain Gage L
Strain Gage G		Strain Gager				
Strain Gage G	-17.78 []	0.00 10	10 9 lbs	0.00 11	0.00 11	

Torsion Tube Combination Loading Data Plot Screen

#### Additional Analysis

**Step 7**. Determine the Bending and Shear Modulus of Elasticity? Why do we need both?

Step 8. Sketch the loading diagrams for this scenario.

Step 9. Calculate the maximum bending and shear stresses for this loading.

**Step 10:** Let's start by analyzing the new bending and shear stresses and strains of our tube using Mohr's Circle as it applies to our rosette strain gages. Compare your results with the restrained tube in Exercise B. Bending and shear stress now play a role due to the tube being unrestrained at the cantilevered end.

**Step 11**: Compare the readings of the axial (top and bottom) strain gages of this test verses to the pure torsional test. Based on just this data, what basic conclusion(s) can be drawn between a tube in pure torsion (restrained on both ends) verses a tube subjected to combination torsion and bending (cantilever configuration).

![](_page_39_Picture_2.jpeg)

#### LAB SESSION #4: Wing Strain Analysis

Strain Gage Placement in Wing (See Page 40 for reference location)

Now that we have some good experience with the TrueStructures<sup>™</sup> System, it's time to tackle the wing structure. Using the knowledge gained analyzing the I-Beam and Tube, you can now see that the wing structure is an advanced combination of beams (spars and ribs) and tube (wing skin).

<u>Step 1</u>. Go back to Lesson #1 and follow the steps outlined in the Introductory Measurement Exercise. The load will be 50 lb applied at the centerline of the wing's front spar. Log the Strain Plot Data (Plot Data Tab).

![](_page_39_Picture_7.jpeg)

Front Spar Load Position

<u>Step 2.</u> Remove the load from the front spar and apply it to the rear spar centerline, following the same data recording steps.

![](_page_40_Picture_3.jpeg)

Rear Spar Load Position

<u>Step 3</u>: Based on the two loading scenarios, compare how the spars and skin are stressed and strained. Use the previous I-Beam and Tube analysis exercises to simplify the basic elements that need to be examined in the wing. State your assumptions and methodology.

#### Additional Analysis

<u>Step 4</u>. For each strain rosette location, use Mohr's Circle to determine the states of stress and strain for each loading scenario (front spar, top and bottom wing skins). Focusing on the front spar rosette results, how do the stress and strain results compare with the corresponding calculations from Step 3?

<u>Step 5.</u> If our wing had a landing gear that transferred 50 lb of load upon touchdown on the runway, which spar would be better suited to mount the gear to, from a load distribution point of view. Why?

<u>Step 6</u>. With the load positioned at the rear spar, calculate the shear stress and consequent shear flow at: Wing Tip and Strain Gage Placements.

<u>Step 7</u>. With the load positioned at the front spar, calculate the shear flow between spar and skin. What would be the minimum rivet spacing required to maintain this structure at this load with no factor of safety?

![](_page_41_Picture_2.jpeg)

Strain Gages are located in the first full bay from spar roots as shown. The two Rosette Strain Gages are located in the center of the bay as indicated by the white hash mark in the photo. An axis indicator is labeled on the back spar for reference (see below)

![](_page_41_Picture_4.jpeg)

Rear Spar has an indicated axis line for strain gages location. All strain gages are located on this axis.